DESIGN AND IMPLEMENTATION OF ADAPTIVE FILTERS FOR REAL TIME APPLICATIONS

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Abstract:
In real time signal processing applications, filtering data requires dedicated hardware to meet challenging time requirements. If the statistics of signal are not known then adaptive filtering algorithms like LMS and RLS can be implemented to estimate the signal statistics iteratively. Adaptive filters are having large range of applications such as noise cancellation, system identification, adaptive linear prediction and beamforming etc. Compared with other digital filters adaptive filter is one whose characteristics can be adapted automatically to get the desired signal.

This article deals with Adaptive noise cancellation application using LMS algorithm and RLS algorithm. An evaluation is made between these two algorithms using MATLAB programming. This application is implemented using VHDL design and the simulation results are obtained by the Xilinx synthesis tool.

Keywords: Adaptive filter, LMS algorithm, RLS algorithm, VHDL

1. INTRODUCTION

For the past many years, adaptive filters design has been an active area of scholarly research and innovative implementations. An adaptive filter is one kind of filter that self-adjusts its coefficients according to an optimizing algorithm. Adaptive filters are essential components in a wide range of signal processing, control, and communications including: 1) signal detection; 2) echo cancellation 3) noise cancellation and/or suppression 3) channel equalization; 4) system identification and inverse modeling of unknown systems; 5) forward and backward predictions and adaptive tracking; and 6) spectral analysis. In many of these applications, the hardware implementations are necessary whenever real-time execution is needed[5].

With the continuous development of the adaptive algorithm application in the digital signal processing field, there are many issues to attract everyone’s attention, including a large amount of computation and the difficult to achieve high-speed and real-time. For a long time, adaptive filtering algorithms are based on the DSP chip, and achieved by the compilation or high-level language programming procedures. This can be a good way to meet the requirements in less demanding situations of real-time, but in the higher real-time requirements occasion and the harsh electromagnetic environment, it has been unable to meet the processing speed and robustness and so on. Field Programmable Gate Array (FPGA) can provide a new method for the hardware implementation of adaptive algorithm through its high flexibility and integration [1].

In this paper in order to explain the performance of LMS algorithm and RLS algorithm, we designed an adaptive noise cancellation application in MATLAB programming and it is implemented in VHDL using ISIM simulator and Xilinx synthesis tool.

The contents of this paper is explained as section 2 describes about adaptive filtering and its algorithms, section 3 describes adaptive noise cancellation application, section 4 describes software simulations and section 5 describes the hardware results.

2. ADAPTIVE FILTERING PROBLEM AND ITS ALGORITHMS:

The goal of any filter is to extract useful information from noisy data. Whereas a normal fixed filter is designed in advance with knowledge of the statistics of both the signal and the unwanted noise, the adaptive filter automatically adjusts to a changing environment through the use of recursive Algorithms. This is useful when either the statistics of the signals are not known before hand of change with time.

Figure 1: Block diagram for the adaptive filter problem.

The discrete adaptive filter (see figure 1) accepts an input $u(n)$ and produces an output $y(n)$ by a convolution with the filters weights, $w(k)$. The desired signal, $d(n)$, is compared with the output to obtain an estimation error $e(n)$. This error signal is used to adjust the filter’s weights automatically for the next time instant. Several adaptive algorithms exist for the weight adjustment, such as the Least Mean Square (LMS) and the Recursive Least Squares (RLS) algorithms.

The choice of training algorithm is dependent upon needed convergence time and the computational complexity available, as statistics of the operating environment [3].
This section briefly describes two of the most recognized adaptive filter design algorithm namely the LMS and the RLS.

**a) LMS algorithm:**

The LMS algorithm is based on the principle of Minimum Mean square error and the steepest descent algorithms. The main advantages of the LMS algorithm is its Computational simplicity, ease of implementation, unbiased convergence, and the existence of a proof in stationary environment. The following mathematical model describes the LMS algorithm [6].

\[ y(n) = w^T(n).x(n) \]
\[ e(n) = d(n) - y(n) \]
\[ w(n+1) = w(n) + \mu e(n)x(n) \]

where \( y(n) \) is the filter output, \( w^T(n) \) is the filter weights in transposed form, \( x(n) \) is the filter inputs, \( d(n) \) is the desired filter output, \( e(n) \) is the error signal which is used for training the filter weights and \( \mu \) is the stepsize factor which is used for controlling the stability and the rate of convergence. The step size must be a small positive value (\( \mu << 1 \)) and \( 0 < \mu < 1/2.N.R \)

Where \( N \) is the number of taps of the filter and \( R \) is the input signal covariance matrix defined as

\[ R = \text{E}[x(n).x^T(n)] \]

**b) RLS algorithm:**

The recursive-least-squares (RLS) algorithm is based on the well-known least squares method. The RLS algorithm recursively solves the least squares problem. In the following equations, the constants \( \lambda \) and \( \delta \) are parameters set by the user that represent the forgetting factor and regularization parameter respectively. The forgetting factor(\( \lambda \)) is a positive constant less than unity, that is roughly a measure of the memory of the algorithm; The vector \( \hat{w} \) represents the adaptive filter’s weight vector and the \( M \)-by-\( M \) matrix \( P \) is referred to as the inverse correlation matrix. The vector \( \pi \) is employed as an intermediary step to computing the gain vector \( k \). This gain vector is multiplied by a priori estimation error \( \xi(n) \) and added to the weight vector to update the weights. Once the weights are updated the inverse correlation matrix is recalculated, and also the training resumes with the new input values. A summary of the RLS algorithm follows:

\[ \Pi(n) = p(n-1) u(n) \]
\[ k(n) = \frac{\Pi(n)}{\lambda + \Pi(n) u^H(n)} \]
\[ \xi(n) = d(n) - \hat{w}H(n-1)u(n) \]
\[ \hat{w}(n) = \hat{w}(n-1) + k(n) \xi(n) \]

and

\[ p(n) = \lambda^{-1} p(n-1) - \lambda^{-1} k(n) uH(n)p(n-1) \]

An adaptive filter trained with the RLS algorithm can converge up to an order of magnitude faster than the LMS filter at the expense of increased computational complexity.

3) ADAPTIVE NOISE CANCELLATION SYSTEM

In adaptive noise cancellation, the adaptive filter is usually designed as a transversal FIR filter structure. The transversal filter consists of three basic elements; unit delay elements, multipliers and adders as shown in Figure 2. The unit delay elements are designed using the unit delay operator . The output of the unit-delay operator \( z^{-1} \) is a delayed copy of its input. The number of delay elements represents the filter order.

![Figure 2. The Transversal FIR Filter Structure](image)

The adaptive noise cancellation filter employing the LMS algorithm can be implemented as shown in Figure 3.

![Figure 3. Adaptive noise cancellation filter](image)

4) SOFTWARE SIMULATION RESULTS

Adaptive noise cancellation is designed by using both LMS algorithm and RLS algorithm. In this we have taken input as sinusoidal signal plus 3 types of noises. those are uniform noise, Gaussian noise and additive white Gaussian noise.
Specifications of LMS and RLS algorithms in MATLAB

- No of filter taps=20
- LMS step size(\( \mu \)) =0.05
- RLS forgetting factor(\( \lambda \)) =0.99
- RLS regularization factor(\( \delta \)) =1
- Initial value of filter coefficients =0

a) Signal corrupted with additive white Gaussian noise

MATLAB LMS Result

MATLAB RLS Result

b) Signal corrupted with uniform noise

MATLAB LMS Result

MATLAB RLS Result

c) Signal corrupted with guassian noise

MATLAB LMS Result
MATLAB RLS result

These results input is the sinusoidal signal plus noise. Learning curve is drawn between mean square error vs. no of iterations. In matlab LMS result the output is converged after 175 iterations while in matlab RLS result the output is converged after 60 iterations only. LMS algorithm takes less no of computations compared with RLS algorithm. Comparison between LMS and RLS is shown in the following table 1.

Table1: comparision between LMS and RLS algorithms

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>No of taps</th>
<th>Total no of iterations</th>
<th>No of iterations to converge</th>
<th>MSE</th>
<th>Computations</th>
</tr>
</thead>
<tbody>
<tr>
<td>LMS</td>
<td>20</td>
<td>400</td>
<td>175</td>
<td>0.024</td>
<td>2N+1</td>
</tr>
<tr>
<td>RLS</td>
<td>20</td>
<td>400</td>
<td>60</td>
<td>0.014</td>
<td>4N²</td>
</tr>
</tbody>
</table>

5) HARDWARE IMPLEMENTATION RESULTS

Adaptive noise cancellation is implemented in VHDL program by using Xilinx synthesis tool. The simulation results are shown in the figure.

Fig 4: convergence of data o/p with i/p data

The schematic diagram of LMS adaptive filter is shown the figure. Here it has 6 inputs and 1 data output. Data_in is 16 bit data, desired data is 16 bit and the data_out is of 16 bit size.

Fig 5: schematic diagram of LMS adaptive filter

Fig 6: RTL schematic diagram of LMS adaptive filter.

Table 2: LMS adaptive filter synthesis results
6) CONCLUSIONS:

This paper uses MATLAB software to design LMS and RLS adaptive filter algorithms and comparison between these two is done. This paper uses a high level language called VHDL to design LMS algorithm for adaptive noise canceller. A desired signal corrupted by additive noise can often be recovered by adaptive noise canceller using the Least Mean Square (LMS) algorithm. In this paper strategies & implementation of Least Mean Square algorithm for adaptive noise canceller is described. The Least Mean Square algorithm was found to be the most efficient training algorithm for FPGA based adaptive filters. Experimental results show that the platform achieves the accuracy and the real-time of the adaptive filter algorithm.

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