

Synthesis of Array of H-plane Tee Junctions of S-band wave guides for the generation of Sum patterns

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Abstract:

In microwave and radar applications shaped or narrow beam patterns are useful. Such radiation patterns can be designed by an array of slot coupled waveguide junctions by using the concept of Taylor distribution method. No literature is available on array of slot coupled H-plane Tee junctions of S band wave guide and no data on such array radiation patterns as reported.

In the present work, an array of H plane Tee junctions of S band wave guide with inclined slots in the narrow wall of primary wave guide are considered and excited with a suitable amplitude distribution. Using recursive formulation of transmission matrix and normalized power balance relation the resonant conductance for a given amplitude distribution are evaluated. The synthesis is carried out by considering a primary guide with matched termination and the amount of incident power absorbed in the terminating load. The results are presented in tabular form.

Introduction:

In guided missiles, supersonic aircrafts and atmospheric entry space vehicles the array of wave guide junctions are very useful, as they desire low profile or flush mounted antennas. In the array design the primary guide feeds cascaded H plane junctions. The radiation pattern obtained from an array of wave guide junctions depends on various parameters like inter element spacing

between the elements, number of elements present in the array, the excitation given to elements and slot parameters (position and inclination of each element, offset displacement from the axis), which provide additional parameters for the array designer.

In the present work, an array of cascaded plane Tee junctions shown in fig 1. are considered and are excited with a suitable amplitude distribution. When the primary guide is matched terminated, the resulting resonant conductance is evaluated for different amounts of incident power delivered to the terminating load, for the number of array elements. An inclined slot in the wave guide radiates cross polarized component, which can be suppressed by slot coupled junctions [1].

Raju et al [1] reported that in estimating the performance of cascaded section of identical junctions, the side lobe levels are found to be high and the radiation pattern cannot be controlled in accordance with the given specification. The realization of desired radiation pattern is possible with junctions which are not identical. The primary guide will be loaded with impedance by each junction in the cascade/ array. The incident and reflected wave at input and output at nth load section are related by transmission matrix [2]. Cascaded section of junctions can be represented by load line shown in fig 1. The impedance due to successive junctions appear in the planes of symmetry of individual sections shown in fig 2. At a

particular frequency, the sections of lines between the consecutive planes are equal to their electrical lines and given by θ_d . The amplitude distribution is obtained by Taylor's method [3]. Das [4] presents an analysis of the cascaded sections of a number of slot-coupled T junctions between rectangular and circular waveguides taking into account the mutual interactions of all possible modes generated by the discontinuities, as well as the effect of wall thickness. The formulation is based on solving a set of coupled integral equations resulting from the boundary conditions at the two interfaces of the waveguide sections representing the coupling slots. Elliot et al [5] derived a general relation between slot voltage and mode voltage is developed, and then formulas are derived for the active, self-reaction and mutual admittances among slots, by considering the mutual coupling for a central slot and a peripheral slot in small arrays if good patterns and impedance are to be obtained. The theory of Stevenson's method, and uses a modified form of Booker's relation based on Babinet's principle to treat nonresonant longitudinal shunt slots in the broad wall of a rectangular waveguide. John [6] analyzed a one-dimensional array comprising tilted edge slots cut in the narrow wall of a rectangular waveguide is presented. The fields in the slots are calculated from a hybrid finite element-boundary integral (FE-BI) equation method. Elliot et al [7] design procedure for arrays of longitudinal slots in one broad wall of each rectangular waveguide is extended to the case that the waveguides have ridges in the opposite broad walls. External mutual coupling has been taken into account.

Formulation:

AMPLITUDE DISTRIBUTIONS:

Different amplitude distributions are used for the reduction of side lobe levels. The

common amplitude distributions are uniform, circular, triangular, cosine and raised cosine on pedestal etc with an objective to reduce the side lobe levels further, another standard distribution represented by raised cosine on pedestal is considered in the present chapter.

The raised cosine on pedestal aperture distribution is represented by

$$A(x) = (1 + 0.48 \cos \pi x), -L \leq x \leq L \quad (1)$$

The second derivative of this equation (1) indicates that the raised cosine on pedestal type of distribution does not contain impulses until the third derivative. It is a gently terminated aperture distribution and it does not exhibit a jump in amplitude at the edges.

The far-field complex radiation pattern due to line source is given by the equation

$$E(u) = \int_{-L}^{+L} A(x) e^{\frac{j2\pi L}{\lambda} xu} dx \quad (2)$$

The raised cosine on pedestal aperture is presented in fig.(3). It is then applied to discrete arrays containing the number of elements equal to $N=20$ and 50 . This is done by considering individual weights of each radiating element. Fig.3. Amplitude distribution of raised cosine on pedestal distribution. The continuous distribution, $A(x)$ is discretized and the resultant excitation levels are shown in figs. (4 & 5) for $N=10$ and 50 . The ordinate indicates the element locations.

These locations are found out using Ishimaru spacing [8]. Radiation patterns are numerically computed for raised cosine on pedestal distribution for discrete arrays containing the number of elements equal to 10 and 50 . The realized patterns in u - domain are presented in figs. (6 & 7).

The incident and reflected waves at the input and output of the n th loaded section are related by the following transmission matrix

$$\begin{bmatrix} I_{n-1} \\ R_{n-1} \end{bmatrix} = \begin{bmatrix} A_{11}^n & A_{12}^n \\ A_{21}^n & A_{22}^n \end{bmatrix} \begin{bmatrix} I_n \\ R_n \end{bmatrix} \text{-----} \quad (3)$$

where $\theta_d = (2\pi/\lambda) d + \pi$, d being the inter element spacing. If P_x is the normalized power delivered to the x th junction and Δ is the fraction of power delivered to the load, it is found

$$\sum_{n=1}^N P_x + \Delta = 1 \text{-----} (4)$$

For inter element spacing equal to $\lambda_g / 2$, the voltage, V appearing across all the elements of Fig. 3 is identical and hence it can be shown that the conductance of x^{th} element is obtained from the formula

$$g_x = \frac{P_x}{\Delta} \text{-----} (5)$$

If a_x is the sampled values of the square of the amplitude distribution curve which is represented as curve of Fig.3 in the locations

$$p_x = \frac{1-\Delta}{\sum_{n=2}^N a_x} \text{-----} (6)$$

The normalized powers P_x appearing in equation (4) are obtained as of the radiating elements,

For matched termination of the array,

$$R_x = 0 \text{ and } I_N^2 = \Delta$$

where N is the total number of junctions, The conductance of the last coupling slot is, hence given by

$$g_N = P_N / I_N^2 \text{-----} (7)$$

Substituting the values of I_N and g_N in equation(1) and solving the set of simultaneous equations

for $P = N, I_{x-1}$ and R_{x-1} are found. Conductance of $(N-1)^{\text{th}}$ junction is given by

$$g_{N-1} = \frac{P_{N-1}}{|I_{N-1} + R_{N-1}|^2} \text{-----} (8)$$

Generating a recursive function in this way. the remaining slot conductance satisfying the amplitude distribution of curve of Fig.1 are evaluated for $d = 0.5\lambda, N=10, 50$ and $\Delta=0.05, 0.1$, Slot parameter resonant length are determined from the data and presented in tabular form.

The method of synthesis described above is quite general and can be applied for the realization of any desired radiation pattern using either an array of waveguide radiators excited through slot coupled junction or an array of slots radiating into free space.

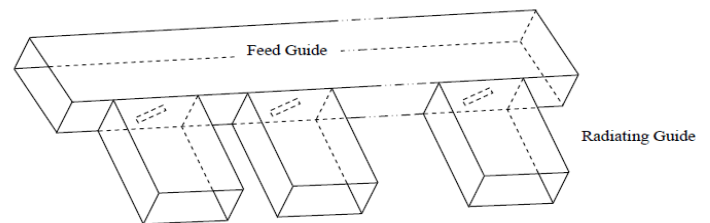


Fig.1 H plane Tee junction array

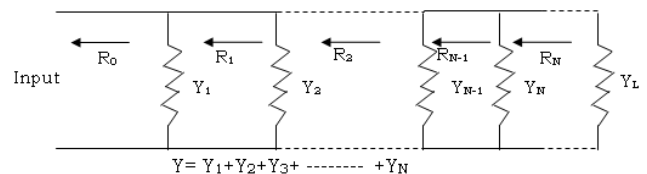


Fig.2. Equivalent circuit of array of slots with matched termination

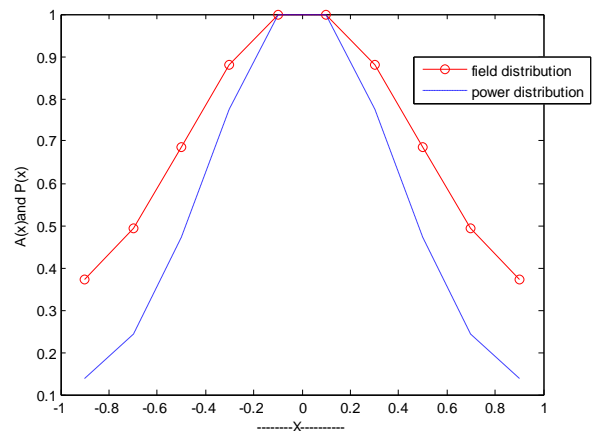


Fig.3. Amplitude and Power distribution for $A(x) = 1 + 0.48 \cos \pi x$

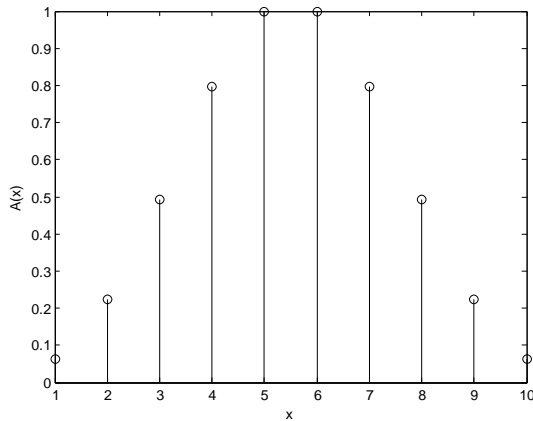


Fig 4 Excitation levels for number of elements = 10

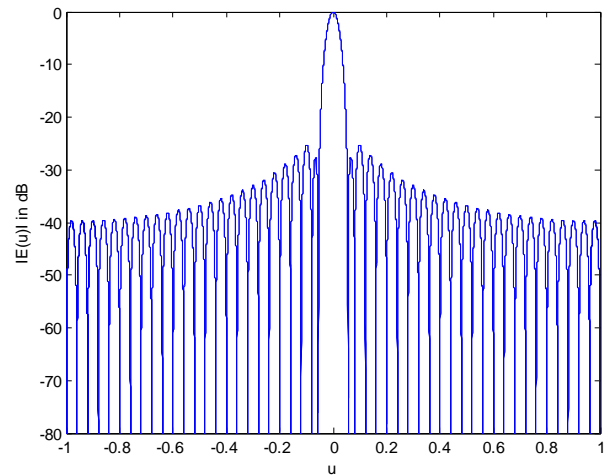


Fig.7. Pattern for discrete array of 50 elements

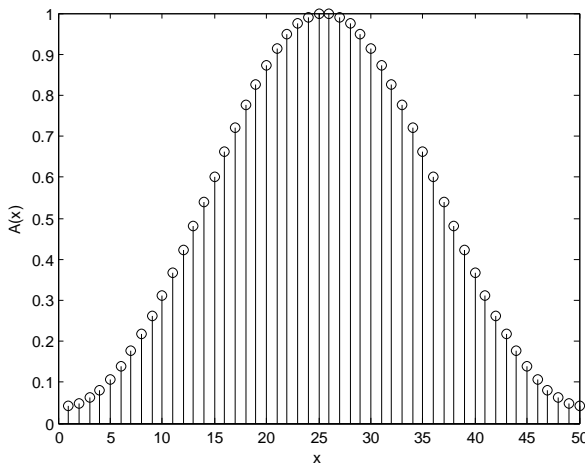


Fig.5 Excitation levels for number of elements = 50

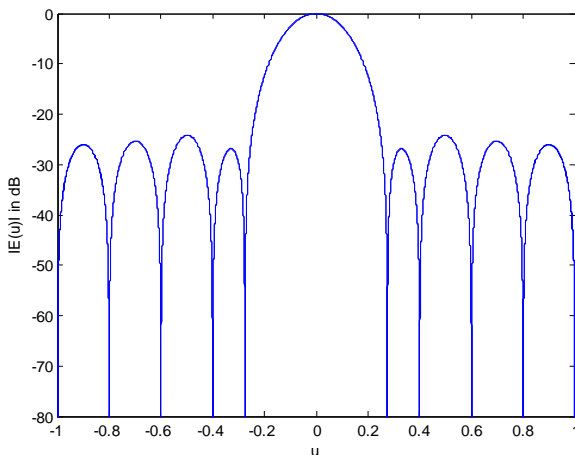


Fig. 6 Pattern for discrete array of 10 elements

Results:

From the expressions of self-reaction and discontinuity in modal current, the admittance parameters are numerically computed for S band H plane Tee junction array. The realized patterns in u-domain using raised cosine on pedestal are presented in figs. (6-7) and the proposed element weights are presented in figs.(5-6). The required conductances of slots to produce the desired radiation patterns are obtained from the expressions. The realized conductances are obtained from the admittance parameter. The required conductance and realized conductance are presented in the tables (1,2,3 and 4). The tabulated results correspond to arrays of 10 and 50 elements. All these results are presented for 0.05 and 0.1 fractional power dissipated in load.

Table.1. array with number of elements N=50, $\Delta=0.05$ and $A(x)=1+0.48 \cos \pi x$

No. of elements	Amplitude level	Required Conductance	realized conductance	Resonant length of slot (cm)
1	0.3731	0.0252	0.0255	5.04
2	0.4929	0.0450	0.0451	5.28
3	0.6866	0.0915	0.0921	5.56
4	0.8803	0.1656	0.1645	5.78
5	1.0000	0.2561	0.2592	5.98
6	1.0000	0.3442	0.3451	6.18
7	0.8803	0.4067	0.4087	6.38
8	0.6866	0.4171	0.4176	6.44
9	0.4929	0.3687	0.3754	6.30
10	0.3731	0.3348	0.3387	6.16

Table.2 array with number of elements $N=10$, $\Delta=0.1$ and $A(x)= 1+0.48 \cos\pi x$

No. of elements	Amplitude level	Required Conductance	realized conductance	Resonant length of slot (cm)
1	0.3731	0.0238	0.0243	5.02
2	0.4929	0.0426	0.0430	5.26
3	0.6866	0.0864	0.0873	5.54
4	0.8803	0.1554	0.1563	5.76
5	1.0000	0.2374	0.2391	5.94
6	1.0000	0.3113	0.3158	6.10
7	0.8803	0.3502	0.3509	6.20
8	0.6866	0.3279	0.3240	6.12
9	0.4929	0.2514	0.2491	5.96
10	0.3731	0.1925	0.1907	5.84

Table.3. array with number of elements $N=50$, $\Delta=0.05$ and $A(x)= 1+0.48 \cos\pi x$

No.of elements	Amplitude level	Required Conductance	realized conductance	Resonant slot length in cm
1	0.3522	0.0046	0.0046	4.32
2	0.3573	0.0048	0.0048	4.34
3	0.3675	0.0051	0.0051	4.36
4	0.3825	0.0055	0.0055	4.40
5	0.4021	0.0061	0.0063	4.46
6	0.4261	0.0069	0.0068	4.50
7	0.4540	0.0079	0.0078	4.56
8	0.4854	0.0091	0.0089	4.62
9	0.5198	0.0106	0.0107	4.70
10	0.5566	0.0123	0.0122	4.76
11	0.5954	0.0142	0.0146	4.84
12	0.6354	0.0164	0.0167	4.90
13	0.6761	0.0189	0.0191	4.96
14	0.7168	0.0217	0.0218	5.02
15	0.7568	0.0247	0.0250	5.08
16	0.7956	0.0280	0.0287	5.14
17	0.8325	0.0315	0.0314	5.18
18	0.8669	0.0353	0.0345	5.22
19	0.8983	0.0393	0.0396	5.38
20	0.9262	0.0434	0.0435	5.32
21	0.9501	0.0478	0.0477	5.36
22	0.9698	0.0523	0.0524	5.40
23	0.9848	0.0569	0.0575	5.44
24	0.9949	0.0616	0.0632	5.48
25	1.0000	0.0663	0.0663	5.50
26	1.0000	0.0710	0.0695	5.52
27	0.9949	0.0756	0.0764	5.56
28	0.9848	0.0802	0.0802	5.58
29	0.9698	0.0845	0.0841	5.60
30	0.9501	0.0886	0.0882	5.62
31	0.9262	0.0924	0.0925	5.64
32	0.8983	0.0958	0.0945	5.65
33	0.8669	0.0986	0.0970	5.66
34	0.8325	0.1009	0.1009	5.70
35	0.7956	0.1025	0.1018	5.68
36	0.7568	0.1034	0.1035	5.69
37	0.7168	0.1034	0.1034	5.69
38	0.6761	0.1026	0.1018	5.68
39	0.6354	0.1010	0.0100	5.70
40	0.5954	0.0986	0.0970	5.66
41	0.5566	0.0956	0.0945	5.65
42	0.5198	0.0922	0.0925	5.64
43	0.4854	0.0886	0.0882	5.62
44	0.4540	0.0850	0.0841	5.60
45	0.4261	0.0818	0.0802	5.58
46	0.4021	0.0794	0.0785	5.57
47	0.3825	0.0780	0.0764	5.56
48	0.3675	0.0781	0.0729	5.54
49	0.3573	0.0710	0.0695	5.52
50	0.3522	0.0663	0.0663	5.50

Table.4. junction array with number of elements
 $N=50$, $\Delta=0.1$ and $A(x)= 1+0.48 \cos\pi x$

No.of elements	Amplitude level	Required Conductance	realized conductance	Resonant slot length in cm
1	0.3522	0.0044	0.0043	4.30
2	0.3573	0.0045	0.0046	4.32
3	0.3675	0.0048	0.0049	4.34
4	0.3825	0.0052	0.0053	4.38
5	0.4021	0.0058	0.0057	4.42
6	0.4261	0.0066	0.0066	4.48
7	0.4540	0.0075	0.0074	4.54
8	0.4854	0.0086	0.0085	4.60
9	0.5198	0.0100	0.0102	4.68
10	0.5566	0.0116	0.0117	4.74
11	0.5954	0.0134	0.0133	4.81
12	0.6354	0.0155	0.0152	4.86
13	0.6761	0.0178	0.0174	4.92
14	0.7168	0.0204	0.0209	5.00
15	0.7568	0.0232	0.0239	5.06
16	0.7956	0.0262	0.0262	5.10
17	0.8325	0.0295	0.0287	5.14
18	0.8669	0.0330	0.0329	5.22
19	0.8983	0.0366	0.0361	5.24
20	0.9262	0.0404	0.0415	5.30
21	0.9501	0.0443	0.0435	5.32
22	0.9698	0.0483	0.0477	5.36
23	0.9848	0.0523	0.0524	5.40
24	0.9949	0.0563	0.0575	5.44
25	1.0000	0.0603	0.0603	5.46
26	1.0000	0.0642	0.0632	5.48
27	0.9949	0.0679	0.0663	5.50
28	0.9848	0.0714	0.0695	5.52
29	0.9698	0.0745	0.0729	5.54
30	0.9501	0.0773	0.0764	5.56
31	0.9262	0.0796	0.0802	5.58
32	0.8983	0.0814	0.0812	5.58
33	0.8669	0.0825	0.0834	5.61
34	0.8325	0.0829	0.0841	5.61
35	0.7956	0.0826	0.0834	5.61
36	0.7568	0.0815	0.0812	5.58
37	0.7168	0.0795	0.0802	5.58
38	0.6761	0.0769	0.0764	5.56
39	0.6354	0.0753	0.0729	5.54
40	0.5954	0.0697	0.0695	5.52
41	0.5566	0.0655	0.0663	5.50
42	0.5198	0.0611	0.0603	5.46
43	0.4854	0.0568	0.0575	5.44
44	0.4540	0.0526	0.0524	5.40
45	0.4261	0.0489	0.0477	5.36
46	0.4021	0.0458	0.0455	5.34

47	0.3825	0.0435	0.0435	5.32
48	0.3675	0.0419	0.0417	5.31
49	0.3573	0.0414	0.0415	5.30
50	0.3522	0.0410	0.0396	5.28

Conclusion:

It is evident from the literature that array of H plane junction formed by S band wave guides are considered for the first time. The arrays are designed with slot coupled junctions to produce narrow beam using tapered amplitude distribution. The proposed distribution is cosine on pedestal. This distribution is found to give a narrow beam of about -25dB. The design adopted in this paper uses recursive formulation, which takes care of internal reflections. A non-radiating port in the array is matched terminated.

Using the analysis presented in preceding chapters the desired conductance of each junction is realized. The resultant radiation patterns for proposed distribution are numerically evaluated and are presented in u-domain.

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